Towards The Estimation Of The Fractal Dimension Of Heart Rate Variability Data

J Hernández Cáceres, H Foyaca Sibat, R Hong, M Sautié, A Namugowa

Abstract

With the aim of determining the Fractal Dimension (FD) of Heart Rate Variability (HRV) signals, three indices (Ix) were evaluated using HRV data. The relationship between each (Ix) and FD was established via a Numerical Experiments (NE) approach. Signals with known FD, were evaluated using different Ix. Once the functional relationship between FD and Ix was found, an estimate of the FD, based on a particular Ix can be proposed (FD_Ix).

The following Ix's were analysed: A) Fractal Dimension estimated by Higuchi's method (FD_H); B) Long Range Slope (LRS), obtained from time detrended data, as well as C) the Autoregressive Dimension Index (ARDI) a measure recently proposed by Enzmann et al. Our results showed that, for fractal signals, a functional dependence between FD and each of the other two Ix's was found in all the cases, explaining more than 96% of the total variance for 1.5-1.95 FD values region. Adding non-fractal components to a pure fractal signal increased FD_Ix. The three indices behaved similarly, i.e. 5-7 % FD_Ix increase in the presence of about 30% of non fractal contribution.

A comparison between FD_Ix of old vs. young subjects revealed a reduction in the FD of the elderly. This is in agreement with literature data, and points to the adequacy of the three methods here proposed.

INTRODUCTION

Fractals are figures and objects that are self-containing in recursive fashion. Fractals can be generated by recursive application of mathematical functions. Any part of the object is a replica of the whole object, but of a smaller size, to infinitesimal levels. The world of fractals is very fascinating. The recursive nature of fractals and how close they resemble natural elements make it an important facet to mathematics and computer graphics. Not only geometrical figures behave as fractals, but also mathematically generated time series behave in a self-similar way. It seems that some processes from the real world (e.g. earthquake and river flooding data, Brownian motions,) may be regarded as fractal time series.

To characterize the entire complex behaviour of a fractal in quantitative terms is a major goal in this area. One of the simplest ways to do so is by fractal dimension (FD) estimation.

For a smooth (i.e., nonfractal) line, an approximate length L(r) is given by the minimum number N of segments of length r needed to cover the line: L(r)=Nr. As r goes to zero, L(r) approaches a finite limit, the length L of the curve.

Similarly one can define the area A or the volume V of nonfractal objects as the limit of an integer power law of r:

\[ A = \lim_{r \to 0} Nr^2 \]
\[ V = \lim_{r \to 0} Nr^3 \]  

Where the integer exponent is the Euclidean dimension E of the object.

This definition cannot be used for fractal objects: as r tends to 0, we enter finer and finer details of the fractal and the product Nr^E may diverge to infinity. However, a real number D exists so that the limit of Nr^D stays finite. This exponent provides an illustration of what the fractal dimension (FD) is. A commonly used practical way to estimate the fractal dimension is the so-called box counting dimension D.
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In the frequency domain, fractal time series exhibit power law properties:

$$ D_H \equiv \lim_{r \to 0} \frac{\log N}{\log(1/r)} $$

Where $PSD$ is the power spectral density, $f$, and the exponent $\gamma$ is the so-called power-spectral index. For the values region between $FD = 1.1$ and $FD = 1.8$ the following relationship between $FD$ and $\gamma$ is valid:

$$ FD = \frac{5 - \gamma}{2} $$

A time series with random phases and power spectrum following the property (2) may be regarded as a synthetic signal with known fractal dimension. Higuchi generated synthetic signals with different values of $\gamma$ (and correspondingly different $FD$ values). This allowed him to propose a reliable method for fractal dimension estimation ($FD_H$).

A common problem in analysing fractal properties of heart rate variability data emerges from the fact that the HRV signal is not a purely fractal process. Available spectral methods present (besides other) the drawback that some FD values from real subjects are beyond the linearity region where (2) is valid (see our results below). Besides, the robustness of $FD_H$ in presence of nonfractal components has not been evaluated so far.

It seems plausible to propose estimates of $FD$ based on different approaches. This perhaps can reduce any method-related bias. At the same time, agreement between methods when real data are being evaluated, as well as providing sense-making differences between groups of subjects may further support their use.

The importance of Heart Rate Variability is in providing a non-invasive and reliable means to assess autonomic nervous function. Heart rate is primarily controlled by the balance between parasympathetic and sympathetic nervous system acting on the intrinsic pacemaker discharge frequency of the sinoatrial node. The normal intervals between heart beats, (only a small fraction of the entire ECG signal) contains a great deal of information about intracardiac and extracardiac processes including its active function controlled by the autonomic nervous system (ANS) as before-mentioned, therefore the heart rate variability (HRV) is an objective procedure used in medicine, especially in the domain of disorders of ANS. A robust HRV research finding is that it is the best predictor of sudden death and for mortality from numerous and diverse medical causes. Its clinical relevance was appreciated when was confirmed that prenatal distress was preceded by alterations in interbeat intervals before any appreciable change occurred in the heart rate itself.

Because HRV can show the status of the autonomic nervous system it can indicate the early degree of deterioration of the ANS in diabetes mellitus, HIV/AIDS, Guillian-Barré syndrome, orthostatic hypotension of the Shy-Drager type in parkinsonism, multiple sclerosis, behavioural disorders, brain injury, as well as in chronic alcoholism, and other possible degenerative neurological conditions. HRV also can be used as a simple tool for monitoring therapeutic effectiveness, and it has become known as a death predictor.

Besides the well-documented relationship between HRV parameters and ANS, there are ample evidences about the presence of fractal properties in the HRV signal. Even when the research on this field is not recent, literature about HRV fractal properties sometimes is contradictory. Besides, hitherto we do not have a physiological counterpart for the putative fractal properties changes observed in different groups of patients. It is our opinion that we need reliable ways of confirming and characterizing the fractal properties of HRV. In this paper, we rely on a numerical experiments approach, where different indices are calculated from synthetic signals whose fractal dimension is known. The original data are “corrupted” with the presence of nonfractal components in order to explore the robustness of these indices for $FD$. Assessment.

In this work we studied three different indices for evaluating the $FD$ in a set of HRV traces:
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- The FDH according to the definition provided by Higuchi.
- The Long Range Slope (LRS) index, a measure of self-similarity obtained from time detrended signals.
- The Autoregressive Dimensional Index (ARDI), obtained from the application of non-linear non-parametric identification analysis to fractal time series.

Even when related to each other, each index is based on a different theoretical grounding.

Prior to the FD estimation from HRV data, numerical experiments were carried out with each of the above-mentioned indices to find:

- The functional relationship between FDH and power law index of synthetic signals whose length was comparable to that of 2-hour HRV data. This was done for confirming that FDH is a reliable FD estimate that can be applied to real HRV signals.
- The other two Ix's were compared to FDH for demonstrating the usefulness in FD estimation.
- The robustness of FD estimates obtained using each method with respect to the presence of non-fractal components in the time series.

We concluded that all the three indices had similar performance for estimating the FD of a time series.

The separate use of each of these indices, as well as their combined use seems to be recommendable for the study of fractal time series with unknown FD. The FD was estimated from HRV traces downloaded from the “Fantasia” database. A set of ten HRV recordings corresponding to 5 young (Y) and 5 elderly (O) clinically healthy male humans was used. We obtained that FD values estimated using each of the three indices, were lower in the group of elderly subjects, when compared to their young counterparts. This is in agreement with data from literature and points to the utility of all the three indices.

MATERIAL AND METHOD

DATA SETS

SIMULATED DATA.

For generating a time series with a known FD value, the methodology introduced by Higuchi was followed. For that purpose, Inverse Fourier Transformed (IFT) was applied to vectors with random phases and spectral densities following (4).

For further details about the procedure for generating fractal time series Higuchi’s article is advised.

By conveniently changing the power law index, a set of simulated signals with FD values ranging from FD = 1.5 to FD = 1.95 was submitted to further analysis.

NON PURELY FRACTAL SYNTHETIC SIGNALS.

For estimating the influence of non fractal sources into the different FD, a fractal signal with FD = 1.85 was mixed at different proportions by adding to a non fractal signal whose spectrum was not equal to zero only at one frequency value (F=3000), and equal to zero elsewhere. The contribution of the non-fractal signal was measured in proportions of total variance. It ranged from 0% to 29% (see table I).

HRV DATA

The database included 10 recordings of intervals between ECG R-waves (I-RR), corresponding to 5 young subjects aged between 21-34 years old (Y), and 5 elderly, 68-81 year old subjects (O). All subjects were rigorously screened and a healthy condition was certified. ASCII files with individual recordings (O1.txt, O2.txt, O5.txt, Y1.txt, Y5.txt) were downloaded from the “Fantasia” database, freely available at “www.physionet.org”. Details about the “Physionet” website, as well as about the possibility to use these data for research purposes are described in Iyengar's manuscript.

Each trace corresponded to an I-RR signal obtained from 2 hours of continuous ECG recording in a supine position, and contained at least 4000 heartbeat counts. The authors of provide a further description about the data.

Signal Analysis

The following indices were estimated from both simulated HRV traces.

FRACTAL DIMENSION FOLLOWING HIGUCHI’S METHOD FD.

Higuchi proposed a method to calculate the fractal dimension of self-similar curves in terms of the slope of the straight line that fits the length of the curve versus the time...
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interval (the lag) in a double logarithmic plot. The method consist of considering a finite set of data taken at a regular interval v(1), v(2), ..., v(N). From this series it may be constructed a new series v(m,k), defined as

\[ v(m), v(m+k), v(m+2k), ..., v(m+[(N-k)/k]k); \] with m=1,2,...,k. (3)

Where \([\text{int}]\) denotes Gauss' notation, that is, the bigger integer, and m,k are integers that indicate the initial time and the time interval respectively. The length of the curve v(m,k) is defined as

Figure 5

Then, the length of the curve for the time interval k is given by mean(L(k)), the average over k sets L(m). Finally, if mean(L(k)) is proportional to \(k^D\), then the curve is fractal with fractal dimension D. We call this estimate FD_HLRS.

LONG RANGE SLOPE (LRS)

LRS is one of the parameters estimated during detrended fluctuation analysis 14. The overall idea of the method is to estimate the roughness of a time series that was previously corrected for any local linear trend. In our version the time series to be analysed is divided into boxes of equal length, n. In each box of length n, a least squares line (or polynomial curve of order k) is fit to the data (representing the trend in that box). Next, the time series is detrended by subtracting the local trend in each box. Then the detrended time series is integrated. The root-mean-square fluctuation of this integrated and detrended time series is calculated and denoted as F(n).

This computation is repeated over all time scales (box sizes), from n = minbox to n = maxbox, to characterize the relationship between F(n), the average fluctuation, and n, the box size. Typically, F(n) will increase with box size n. A linear relationship on a log-log plot indicates the presence of power law (fractal) scaling. Under such conditions, the fluctuations can be characterized by a scaling exponent, i.e., the slope of the line relating log[F(n)] to log[n]. It has been shown that in HRV data instead of a continuous line, we observe two lines with a breakpoint. One line correspond to short duration boxes (e.g. n<5), whereas the second corresponds to boxes with n>7. The slope of the long range segment (LRS) was considered in our computations. There is one difference between our procedure and that of 13. In the original version, the signal is integrated prior to be detrended. However, our version proved to have a high predictive power in predicting haemodynamic instability among haemodialysis patients 14.

AUTOREGRESSIVE DIMENSION INDEX (ARDI)

Enzmann et al.15, firstly introduced this index as a measure for evaluating HRV in patients under haemodialysis treatment. The rationale of the method is to apply a nonlinear identification approach to nonstationary data. Nonlinear identification has proven to be adequate for the analysis of short duration (180-500 data points) time series whose dynamical nature is unknown 16. The method allows to separate the deterministic and stochastic components of a stochastic nonlinear system. In particular, most of the known classical chaotic attractors could be reproduced by this method 17. It can be viewed either as an extension of classical linear autoregressive estimation to the nonlinear case or either as an extension of classical chaos theory approach to the case when the nonlinear system is fed by innovation noise 18,19. From all the wealth of information that is obtained by this method we selected a single parameter, namely, the optimal order of the autoregressive model.

For ARDI estimation a recording of duration N = 5000 was divided into 25 non overlapping segments 200 data points long each. To each segment the following non-linear autoregressive model was fit:

\[ I_n = f(I_{n-1}, I_{n-2}, ..., I_{n-r}) + \gamma_n \] (5)

Where \(I_{n-1}, I_{n-2}, ..., I_n\) are the n-th, (n-1)-th... R-R intervals in the sequence.

\(f\) is a multivariate non-linear function relating the nth interval to the k preceding intervals in the sequence.\{\gamma_n\} corresponds to a random, independent, identically distributed variable. The parameter r is the order of the non-linear autoregressive model. The function F is estimated non-parametrically 20.

According to this method, the estimate of \(f\) at an arbitrary point \((Z_{n+1}, Z_{n+2}, ..., Z_{n+r})\) of the state space is obtained as a weighted average of the data.
The bandwidth parameter $h$ determines the weight of each neighbouring point in the phase space. In particular, if his too large we have just averaging, whereas for a too short $h$ noise will be incorporated into the deterministic function. A cross minimal validation error criterion has been used for selecting the bandwidth parameter (17,18,19 , Caceres, los 3 papers, peter folklore). The determination of the optimal order of an autoregressive model is difficult task even for parametric models. The introduction of likelihood criteria is an attempt to penalize the good prediction at expenses of too many parameters. For that purpose a cross validation criterion has also been used (17, 18, 19). For a description of the use of cross validation in kernel; nonlinear autorregression the reader is refered to [21].

After computing the optimal order $r$ for each segment of the whole trace it is possible to compute ARDI as the proportion of $r$-values equal or higher than 15 corresponds to ARDI.

$$\text{ARDI} = \frac{\text{Number of segments with optimal order higher than 15}}{\text{Total number of segments}}.$$ 

ESTIMATION OF FRACTAL DIMENSION VIA INDEX EVALUATION

For estimating the fractal dimension on the basis of a particular index ($\text{FD}_{\text{Ix}}$), NE was carried out. $\text{FD}_{\text{LRS}}$ and $\text{FD}_{\text{ARDI}}$ were considered, whereas $\text{FD}_{h}$ was taken as the “golden rule”.

At least 10 simulated signals with FD ranging from FD=1.1 to FD=2.0 were submitted to the estimation of each index. The dependence of FD respect to each Ix was fit to a polynomial

$$\text{FD} = P_i (Ix) \quad (7)$$

Where $i$ is the degree of the polynomial $P$.

Accordingly, the FD of a given time series was obtained via estimating each index and applying (7). For $\text{FD}_{h}$, a 3rd degree polynomial was used linear regression was used for estimating $\text{FD}_{\text{LRS}}$, and 5th degree polynomial was used for $\text{FD}_{\text{ARDI}}$.

STATISTICAL ANALYSIS

Mean and standard deviation for $\text{FD}_{h}$, $\text{FD}_{\text{LRS}}$, $\text{FD}_{\text{ARDI}}$ were obtained for both the Y and O groups. Conventional analysis under Gaussianity assumption was carried out.

Nonparametric permutation analysis is recommended for small samples with unknown distribution. For each index, all the 10 individual values from the Y and O traces were allocated according to all possible permutations into 2 groups with 5 individuals each. The difference between the mean values for each randomly generated pair of groups was computed. An empirical distribution for the differences between the means was generated. Accordingly, the probability for the mean difference between Y and O the corresponding null hypothesis ($H_0$) of no differences was tested.

RESULTS

NUMERICAL EXPERIMENTS.

We first tried to reproduce the numerical experiments performed by Higuchi for the case when the duration of the segment is relatively short ($N=5000$). We obtained that in the FD values region from 1.1 to 1.9 the values corresponded nicely to the power law index values ($\gamma$) in accordance with the theoretically expected relationship (2). Our regression yielded:

$$\text{FD}_{h} = 2.48 - 0.46\gamma \quad (n=87, r=0.97); \quad (8)$$

Thus we regard this result as supporting the validity of $\text{FD}_{h}$ as an estimate for FD.

Previous results from our laboratory suggested that FD values for HRV data are expected in the 1.7 – 1.9 values region. As the result of the NE carried out, the following relationships were found in that FD-values region:

- $\text{FD} = 2.13636 - 1.363636*(\text{LRS}) \quad (n=9, r = -0.96) \quad (9)$
- $\text{FD} = 1.917338 + 0.0098492*(\text{ARDI}) - 0.0007324*(\text{ARDI})^2 + 0.0000156*(\text{ARDI})^3 - 1.105*10^{-7}*(\text{ARDI})^4 + 4.02*10^{-9}*(\text{ARDI})^5 \quad (n=20, 95 \% \text{ of the variance explained}) \quad (10)$

The relation between ARDI and FD is illustrated in fig (1). $\text{FD}_{\text{LRS}}$ and $\text{FD}_{\text{ARDI}}$ are obtained from (8) and (9) respectively.
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Figure 7
Figure 1: Relationship between FD and ARDI. Each point corresponds to the Fractal Dimension evaluated from a simulated signal whose ARDI had been previously estimated.

The degree of concordance between different FD estimates was high when purely fractal signals were evaluated, thus for $\text{FD}_{\text{ARDI}}$ and $\text{FD}_{\text{PLI}}$ the correlation coefficient was $r = 0.96$ (n=10).

Addition of a non-fractal signal to a purely fractal signal was a cause for FD increase with all the three indices. As shown in table I, adding up to about 30% of a non-fractal component to the total variance increases the estimated FD value in about 5-7%. According to different authors, real HRV data contain about 20% of non-fractal contribution to the overall variance. At the same time, it seems plausible to expect that most of the clinical conditions related to changes in the spectral peaks (LF, and HF) imply changes in the range from the “normal” value of 22% to lower values around 18 %. Following the results shown in table I, it means that changes in nonfractal spectral peaks may not account for more than a 1% change in FD values estimated by any of these indices. Thus, our results suggest that all the three proposed FD estimates might be pertinent for HRV fractal dimension evaluation.

Figure 8
Table I: Percent change in different FD as results of adding a non-fractal component to a purely fractal signal (FD = 1.85) HRV data: In table II the estimates of FD according to each index are shown for each of the HRV recording analysed.

<table>
<thead>
<tr>
<th>% non fractal variance added</th>
<th>$\text{FD}_{\text{HR}}$</th>
<th>$\text{FD}_{\text{RS}}$</th>
<th>$\text{FD}_{\text{ARDI}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>100</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>1</td>
<td>100</td>
<td>101</td>
<td>100</td>
</tr>
<tr>
<td>10</td>
<td>102</td>
<td>102</td>
<td>101</td>
</tr>
<tr>
<td>15</td>
<td>105</td>
<td>105</td>
<td>101</td>
</tr>
<tr>
<td>20</td>
<td>105</td>
<td>106</td>
<td>108</td>
</tr>
</tbody>
</table>

Figure 9
Table II: FD values for the 10 recordings from the “Fantasia” database. Recording’s codes correspond to the original file names as presented at the website.

<table>
<thead>
<tr>
<th>Recording’s code</th>
<th>$\text{FD}_{\text{HR}}$</th>
<th>$\text{FD}_{\text{RS}}$</th>
<th>$\text{FD}_{\text{ARDI}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>O</td>
<td>1.64</td>
<td>1.85</td>
<td>1.60</td>
</tr>
<tr>
<td>O</td>
<td>1.49</td>
<td>1.50</td>
<td>1.35</td>
</tr>
<tr>
<td>O</td>
<td>1.46</td>
<td>1.45</td>
<td>1.35</td>
</tr>
<tr>
<td>O</td>
<td>1.62</td>
<td>1.88</td>
<td>1.60</td>
</tr>
<tr>
<td>O</td>
<td>1.70</td>
<td>1.50</td>
<td>1.65</td>
</tr>
<tr>
<td>Y</td>
<td>1.11</td>
<td>1.0</td>
<td>1.10</td>
</tr>
<tr>
<td>Y</td>
<td>1.47</td>
<td>1.15</td>
<td>1.30</td>
</tr>
<tr>
<td>Y</td>
<td>1.56</td>
<td>1.0</td>
<td>1.45</td>
</tr>
<tr>
<td>Y</td>
<td>1.29</td>
<td>1.22</td>
<td>1.30</td>
</tr>
<tr>
<td>Y</td>
<td>1.36</td>
<td>1.30</td>
<td>1.30</td>
</tr>
</tbody>
</table>

(In table III, a summary is provided for the statistical processing of the data).

Figure 10
Table III: Means standard deviations and type I error probabilities for the groups O and Y. In the case of permutations the probability $P_0$ that the difference between the means of the both groups is zero has been computed.

<table>
<thead>
<tr>
<th>Group</th>
<th>$\text{FD}_{\text{HR}}$</th>
<th>$\text{FD}_{\text{RS}}$</th>
<th>$\text{FD}_{\text{ARDI}}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>O</td>
<td>1.07(±0.04)</td>
<td>1.91(±0.17)</td>
<td>1.99(±0.02)</td>
</tr>
<tr>
<td>Y</td>
<td>1.89(±0.07)</td>
<td>1.92(±0.08)</td>
<td>1.94(±0.06)</td>
</tr>
</tbody>
</table>

According to the three indices considered FD is decreased in the group of elderly subjects. Statically significant differences were obtained using either conventional or nonparametric permutation analysis. These results agree with ample literature evidence mainly using other estimation methods.

DISCUSSION
Here three indices for time domain estimation of FD in HRV data were proposed. Higuchi had previously proposed one of these indices. The second index (LRS) is a modification of the original DFA method. This index exhibits good predictive capability and has been used by our group for few years. The third index appeared from our early attempts to characterize HRV by a non-linear identification approach.

As our result revealed, the two indices are functionally related to fractal dimension when purely fractal signals were analysed. The robustness of all three indices was similar. However, we do agree that more specific numerical experiments are needed for a more complete characterization of these indices’ robustness.

All the three indices documented in a similar way a result with ample literature report: the decrease with age of FD from HRV recordings.
A further step in our research might be the possibility to use these estimates for assessing FD from short duration traces, as well as from traces sampled at lower frequencies. Our preliminary results (not shown) point to a preservation of the predictive power of these estimates even for 2-min duration traces, whereas only one of the indices (FDₙ) loses its clinical predictability as the sampling frequency is reduced from 1000 to 100 Hz.

Recent experience with the advent of chaos theory shows that we must be extremely cautious when trying to apply results of mathematical theories into real objects. An avalanche of chaos “demystification” followed the early “epidemics” of chaos finding in almost any area of physiology and the sad sensation that our understanding of different physiological mechanisms remains obscure had become a reason for pessimism.

In our opinion, the sole use of power spectrum measures for assessing the putative fractality of a time series whose mechanism is unknown may appear misleading. Even with mathematical objects this can take place. One example is the known intermittent Pomeau-Manneville map. This map is a deterministic non-linear low dimensional processes. However, its power spectrum is indistinguishable from that of a typical fractal with “1/f” noise. The non-linear identification approach (from which ARDI is derived) is capable of distinguishing the both. Thus we may expect that these indices will provide not only new ways for assessing HRV fractal properties, but also for understanding some of HRV underlying dynamics.

The fractal properties of HRV may open avenues for radically new promising views to the heart beat regulation. Concepts as self-organized criticality may bring us to the conceptual frames of the feedback theory scenarios. However, for these views being productive, we need a simple conviction: that fractal-like processes take place in the human body. Our work has been an attempt in that direction.

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